

```

In[ ]:= RandSelfadjMatrix[l_] := Module[{A, i},
  A = RandomVariate[NormalDistribution[], {l, l}] +
    I * RandomVariate[NormalDistribution[], {l, l}];
  A = A + ConjugateTranspose[A];
  A = Chop[A];
  A]

In[ ]:= RandPositive[l_, r_] := Module[{A},
  A = RandomVariate[NormalDistribution[], {l, r}] +
    I * RandomVariate[NormalDistribution[], {l, r}];
  A = A.ConjugateTranspose[A];
  A]

RandState[l_, r_] := Module[{A},
  A = RandPositive[l, r];
  A = A / Tr[A];
  A]

In[ ]:= CostfromObservable[Observables_, transpose_] := Sum[
  MatrixPower[KroneckerProduct[Observables[[k]], IdentityMatrix[Length[Observables[[1]]]]] -
    KroneckerProduct[IdentityMatrix[Length[Observables[[1]]]], If[transpose,
      Transpose[Observables[[k]], Observables[[k]]], 2], {k, 1, Length[Observables]}]

In[ ]:= SaMCNB[dim_] :=
  SaMCNB[dim] = Flatten[{{Table[SparseArray[{{k, k} → 1, {dim, dim} → 0}], {k, 1, dim}]],
    Table[Table[SparseArray[{{k, m} → Sqrt[2] / 2, {m, k} → Sqrt[2] / 2, {dim, dim} → 0}],
      {m, k + 1, dim}], {k, 1, dim - 1}], Table[Table[SparseArray[{{k, m} → -I * Sqrt[2] / 2,
      {m, k} → I * Sqrt[2] / 2, {dim, dim} → 0}], {m, k + 1, dim}], {k, 1, dim - 1}]], 2];

In[ ]:= SaMPB[2] = {{{1, 0}, {0, 1}}, {{0, 1}, {1, 0}}, {{0, -I}, {I, 0}}, {{1, 0}, {0, -1}}};
SaMPB[dim_] := SaMPB[dim] = Flatten[Table[
  KroneckerProduct[SaMPB[dim / 2][[j]], SaMPB[2][[k]], {j, 1, dim^2 / 4}, {k, 1, 4}], 1];

In[ ]:= SaMPNB[dim_] := SaMPNB[dim] = SaMPB[dim] / Sqrt[dim];

```

```

In[ ]:= QOT[ρ_, ω_, C_, dual_, transpose_] := Module[{dim, sol, Π, x, y, X, Y},
  dim = Length[ρ];
  If[
    dual, {x = Table[Symbol["x" <> ToString[n]], {n, dim^2}];
    y = Table[Symbol["y" <> ToString[n]], {n, dim^2}];
    sol = SemidefiniteOptimization[-Tr[(y.SaMCNB[dim]).ω + (x.SaMCNB[dim]).ρ],
      {VectorGreaterEqual[{C - KroneckerProduct[(y.SaMCNB[dim]), IdentityMatrix[dim]] -
        KroneckerProduct[IdentityMatrix[dim], If[transpose, Transpose[
          (x.SaMCNB[dim])], x.SaMCNB[dim]]}, 0}, {"SemidefiniteCone", dim^2}]}},
    Flatten[{x, y}]]];
  X = Chop[sol[[1 ;; dim^2, 2]].SaMCNB[dim], 10^-3];
  Y = Chop[sol[[dim^2 + 1 ;; 2 * dim^2, 2]].SaMCNB[dim], 10^-3];
  Chop[Sqrt[Tr[X.ω + Y.ρ]], 10^-3], X // MatrixForm, Y // MatrixForm},

  {x = Table[Symbol["x" <> ToString[n]], {n, dim^4}];
  sol = SemidefiniteOptimization[Chop[Simplify[Tr[(x.SaMCNB[dim^2]).C]], 10^-3],
  {ResourceFunction["MatrixPartialTrace"][x.SaMCNB[dim^2], 2, {dim, dim}] == ω,
    ResourceFunction["MatrixPartialTrace"][x.SaMCNB[dim^2], 1, {dim, dim}] ==
      If[transpose, Transpose[ρ], ρ],
    VectorGreaterEqual[{x.SaMCNB[dim^2], 0}, {"SemidefiniteCone", dim^2}]}},
  x];
  Π = Chop[Sum[sol[[n, 2]].SaMCNB[dim^2] [[n]], {n, 1, dim^4}], 10^-3];
  Chop[Sqrt[Tr[C.Π]], 10^-3], Π // MatrixForm]]]

In[ ]:= ModQOT[ρ_, ω_, cost_, dual_, transpose_] := Sqrt[QOT[ρ, ω, cost, dual, transpose] [[1]]^2 -
  (QOT[ρ, ρ, cost, dual, transpose] [[1]]^2 + QOT[ω, ω, cost, dual, transpose] [[1]]^2) / 2]

In[ ]:= TriIneq[ρ_, ω_, τ_, C_, dual_, transpose_] := ModQOT[ρ, ω, C, dual, transpose] +
  ModQOT[ω, τ, C, dual, transpose] - ModQOT[ρ, τ, C, dual, transpose]

```

```

In[ ]:= ρ01 = 1 / 2 * {1, 1 / Sqrt[2], 1 / Sqrt[3], 0}.SaMPB[2]

```

```

Out[ ]:=  $\left\{ \left\{ \frac{1}{2}, \frac{1}{2} \left( \frac{1}{\sqrt{2}} - \frac{i}{\sqrt{3}} \right) \right\}, \left\{ \frac{1}{2} \left( \frac{1}{\sqrt{2}} + \frac{i}{\sqrt{3}} \right), \frac{1}{2} \right\} \right\}$ 

```

```

In[ ]:= τ01 = 1 / 2 * {1, 0, 1 / 3, 1 / 4}.SaMPB[2]

```

```

Out[ ]:=  $\left\{ \left\{ \frac{5}{8}, -\frac{i}{6} \right\}, \left\{ \frac{i}{6}, \frac{3}{8} \right\} \right\}$ 

```

```

In[ ]:= step1 = 0.01;

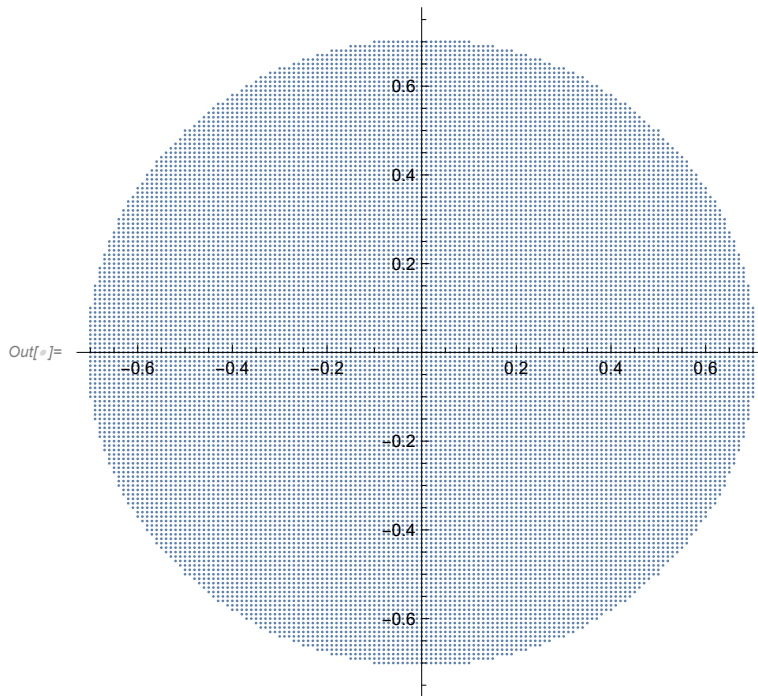
```

```

In[ ]:= coordinates1 = Select[Flatten[Table[{x, y}, {x, -1, 1, step1}, {y, -1, 1, step1}], 1],
  PositiveSemidefiniteMatrixQ[1 / 2 * (Flatten[{1, #, 1 / Sqrt[2]}]).SaMPB[2]] &];

```

```
In[ ]:= ListPlot[coordinates1, AspectRatio -> 1]
```



```
In[ ]:= Cost1 = CostfromObservable[SaMPB[2][{2, 4}], True]
```

```
Out[ ]:= {{2, 0, 0, -2}, {0, 6, -2, 0}, {0, -2, 6, 0}, {-2, 0, 0, 2}}
```

```
In[ ]:=  $\omega_1 = 1 / 2 * (\text{Flatten}[\{1, \#, 1 / \text{Sqrt}[2]\}]) . \text{SaMPB}[2] \& / @ \text{coordinates1};$ 
```

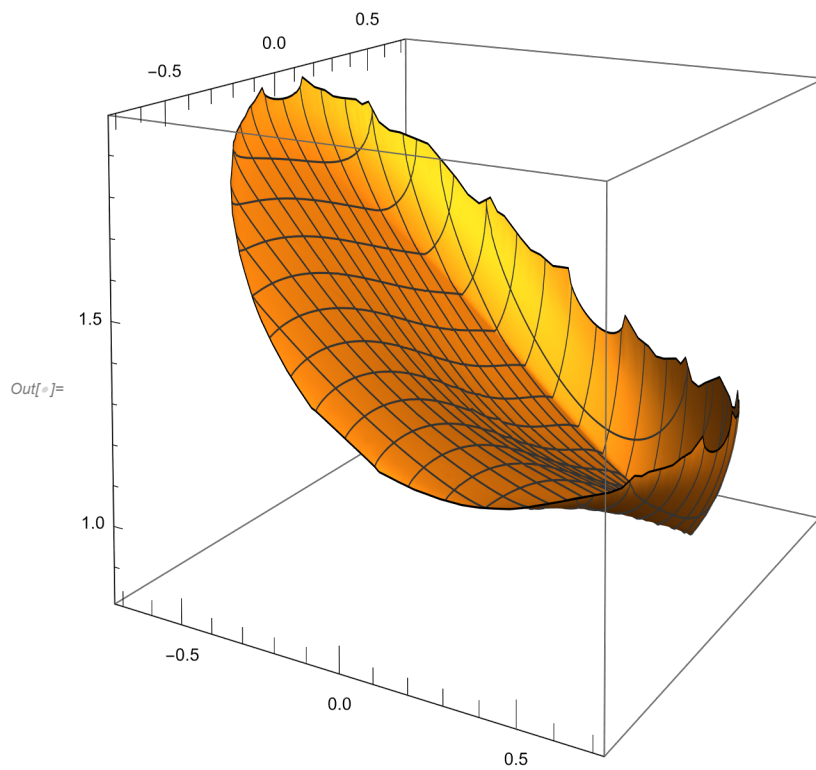
```
In[ ]:= Off[SemidefiniteOptimization::parsuc]
```

```
In[ ]:= {time1, result1} = AbsoluteTiming[TriIneq[ $\rho_0$ , #,  $\tau_0$ , Cost1, False, True] & / @  $\omega_1$ ];
```

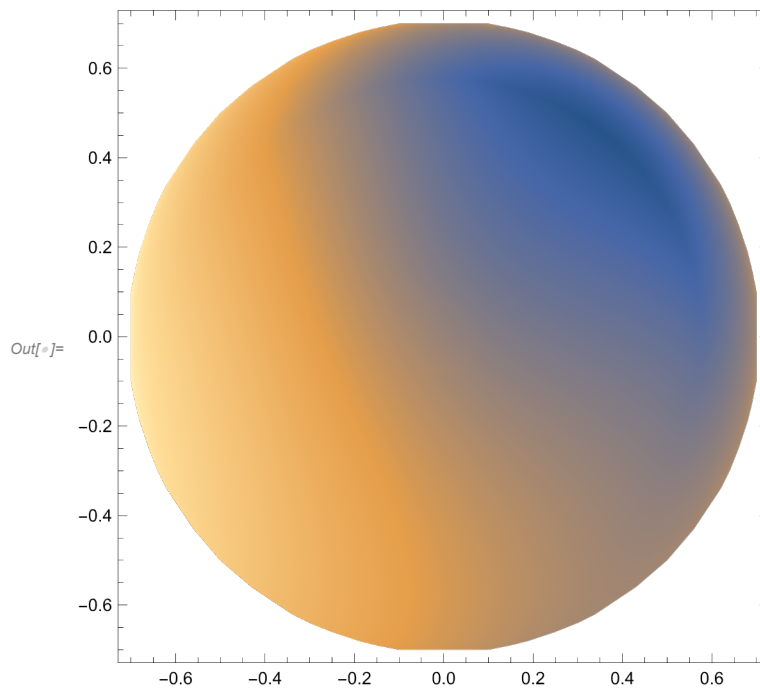
```
In[ ]:= time1 / 3600
```

```
Out[ ]:= 0.666655
```

```
In[7]:= ListPlot3D[Join[coordinates1, Transpose@{result1}, 2], AspectRatio -> 1]
```



```
In[8]:= ListDensityPlot[Join[coordinates1, Transpose@{result1}, 2], AspectRatio -> 1]
```



```
In[9]:= Max[Abs[Im[result1]]]
```

Out[9]= 0


```
In[ ]:= Min[result1]
```

```
Out[ ]:= 0.832397
```

```
In[ ]:= ρ02 = 1 / 4 * {1, 0, 0, 0, 0, 0.1, 0, 0, 0.2, 0, 0, 0, 0.3, 0, 0, 0}.SaMPB[4]
```

```
Out[ ]:= {{0.325 + 0. i, 0. + 0. i, 0. - 0.05 i, 0.025 + 0. i},
          {0. + 0. i, 0.325 + 0. i, 0.025 + 0. i, 0. - 0.05 i},
          {0. + 0.05 i, 0.025 + 0. i, 0.175 + 0. i, 0. + 0. i},
          {0.025 + 0. i, 0. + 0.05 i, 0. + 0. i, 0.175 + 0. i}}
```

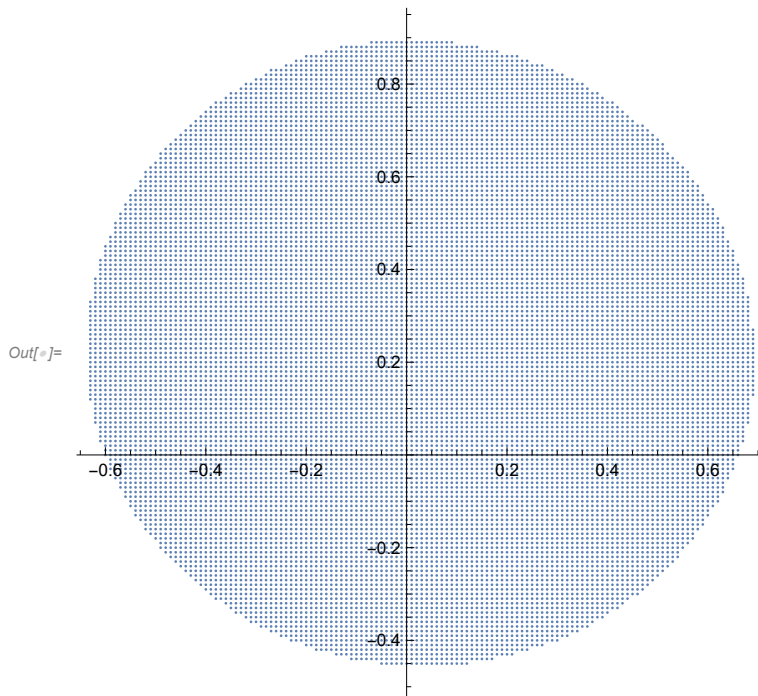
```
In[ ]:= τ02 = 1 / 4 * {1, 0, 0, 0.3, 0, 0, 0, 0.2, 0, 0, 0, 0, 0.1, 0, 0, 0}.SaMPB[4]
```

```
Out[ ]:= {{0.35 + 0. i, 0. + 0. i, 0.05 + 0. i, 0. + 0. i}, {0. + 0. i, 0.2 + 0. i, 0. + 0. i, -0.05 + 0. i},
          {0.05 + 0. i, 0. + 0. i, 0.3 + 0. i, 0. + 0. i}, {0. + 0. i, -0.05 + 0. i, 0. + 0. i, 0.15 + 0. i}}
```

```
In[ ]:= step2 = 0.01;
```

```
In[ ]:= coordinates2 = Select[Flatten[Table[{x, y}, {x, -1, 1, step2}, {y, -1, 1, step2}], 1],
                             PositiveSemidefiniteMatrixQ[
                               1 / 4 * (Flatten[{1, #, 0, 0.1, 0.1, 0.1, 0, 0.3, 0, 0.2, 0, 0, 0, 0, 0}].SaMPB[4]) &];
```

```
In[ ]:= ListPlot[coordinates2, AspectRatio -> 1]
```



```
In[ ]:= Cost2 = CostfromObservable[SaMPB[4][[2 ;; 16]], True]
```

```
Out[ ]:= { {24, 0, 0, 0, 0, -8, 0, 0, 0, 0, -8, 0, 0, 0, 0, -8},
  {0, 32, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}, {0, 0, 32, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0},
  {0, 0, 0, 32, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}, {0, 0, 0, 0, 32, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0},
  {-8, 0, 0, 0, 0, 24, 0, 0, 0, 0, -8, 0, 0, 0, 0, -8},
  {0, 0, 0, 0, 0, 0, 32, 0, 0, 0, 0, 0, 0, 32, 0, 0}, {0, 0, 0, 0, 0, 0, 0, 32, 0, 0, 0, 0, 0, 0, 32, 0},
  {0, 0, 0, 0, 0, 0, 0, 0, 32, 0, 0, 0, 0, 0, 0, 32}, {0, 0, 0, 0, 0, 0, 0, 0, 0, 32, 0, 0, 0, 0, 0, 32},
  {-8, 0, 0, 0, 0, -8, 0, 0, 0, 0, 24, 0, 0, 0, 0, -8},
  {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 32, 0, 0, 0, 0, 32}, {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 32, 0, 0, 0, 32},
  {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 32, 0, 0, 0}, {0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 32, 0, 32},
  {-8, 0, 0, 0, 0, -8, 0, 0, 0, 0, -8, 0, 0, 0, 0, 24} }
```

```
In[ ]:= Cost2 // MatrixForm
```

```
Out[ ]:= MatrixForm=
```

```
( 24 0 0 0 0 -8 0 0 0 0 -8 0 0 0 0 -8
  0 32 0 0 0 0 0 0 0 0 0 0 0 0 0 0
  0 0 32 0 0 0 0 0 0 0 0 0 0 0 0 0
  0 0 0 32 0 0 0 0 0 0 0 0 0 0 0 0
  0 0 0 0 32 0 0 0 0 0 0 0 0 0 0 0
 -8 0 0 0 0 24 0 0 0 0 -8 0 0 0 0 -8
  0 0 0 0 0 0 32 0 0 0 0 0 0 0 0 0
  0 0 0 0 0 0 0 32 0 0 0 0 0 0 0 0
  0 0 0 0 0 0 0 0 32 0 0 0 0 0 0 0
  0 0 0 0 0 0 0 0 0 32 0 0 0 0 0 0
 -8 0 0 0 0 -8 0 0 0 0 24 0 0 0 0 -8
  0 0 0 0 0 0 0 0 0 0 0 32 0 0 0 0
  0 0 0 0 0 0 0 0 0 0 0 0 32 0 0 0
  0 0 0 0 0 0 0 0 0 0 0 0 0 32 0 0
  0 0 0 0 0 0 0 0 0 0 0 0 0 0 32 0
 -8 0 0 0 0 -8 0 0 0 0 -8 0 0 0 0 24 )
```

```
In[ ]:=  $\omega_2 = 1 / 4 * (\text{Flatten}[\{1, \#, 0, 0.1, 0.1, 0.1, 0, 0.3, 0, 0.2, 0, 0, 0, 0, 0\}]) \cdot \text{SaMPB}[4] \ \& \ /@$ 
  coordinates2;
```

```
In[ ]:= Off[SemidefiniteOptimization::parsuc]
```

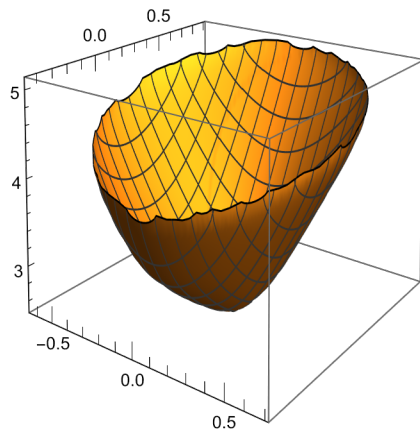
```
In[ ]:= {time2, result2} = AbsoluteTiming[TriIneq[ $\rho_0$ 2, #,  $\tau_0$ 2, Cost2, False, True] & /@  $\omega_2$ ];
```

```
In[ ]:= time2 / 3600
```

```
Out[ ]:= 13.1223
```

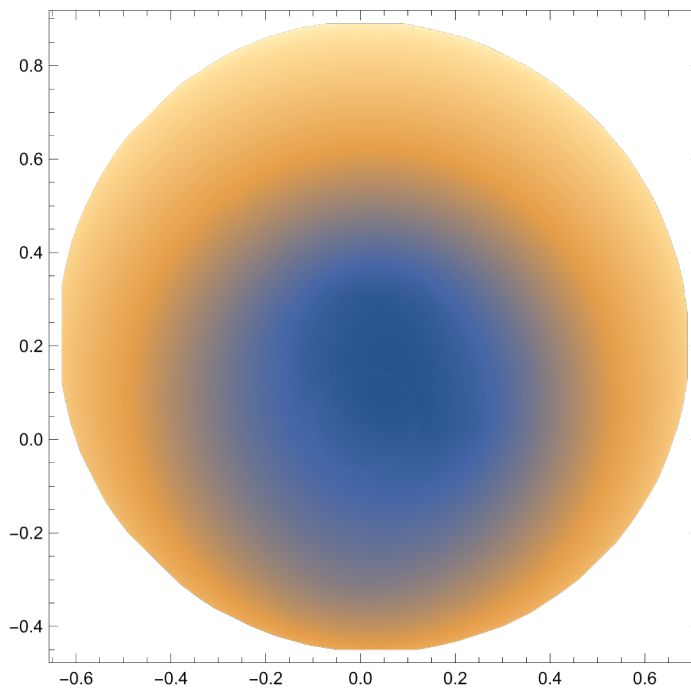
```
In[6]:= ListPlot3D[Join[coordinates2, Transpose@{result2}, 2], AspectRatio -> 1]
```

Out[6]=



```
In[7]:= ListDensityPlot[Join[coordinates2, Transpose@{result2}, 2], AspectRatio -> 1]
```

Out[7]=



```
In[8]:= Max[Abs[Im[result2]]]
```

Out[8]= 0

```
In[9]:= Min[result2]
```

Out[9]= 2.51399

```
In[10]:= rho3 = RandState[2, 2]
```

Out[10]= {{0.873149 + 0. i, -0.279734 + 0.0887207 i}, {-0.279734 - 0.0887207 i, 0.126851 + 0. i}}

```
In[ ]:= % // MatrixForm
```

```
Out[ ]//MatrixForm=
```

$$\begin{pmatrix} 0.873149 + 0. i & -0.279734 + 0.0887207 i \\ -0.279734 - 0.0887207 i & 0.126851 + 0. i \end{pmatrix}$$

```
In[ ]:= τ03 = RandState[2, 2]
```

```
Out[ ]:= { {0.941077 + 0. i, -0.204803 + 0.0294567 i}, {-0.204803 - 0.0294567 i, 0.0589231 + 0. i} }
```

```
In[ ]:= % // MatrixForm
```

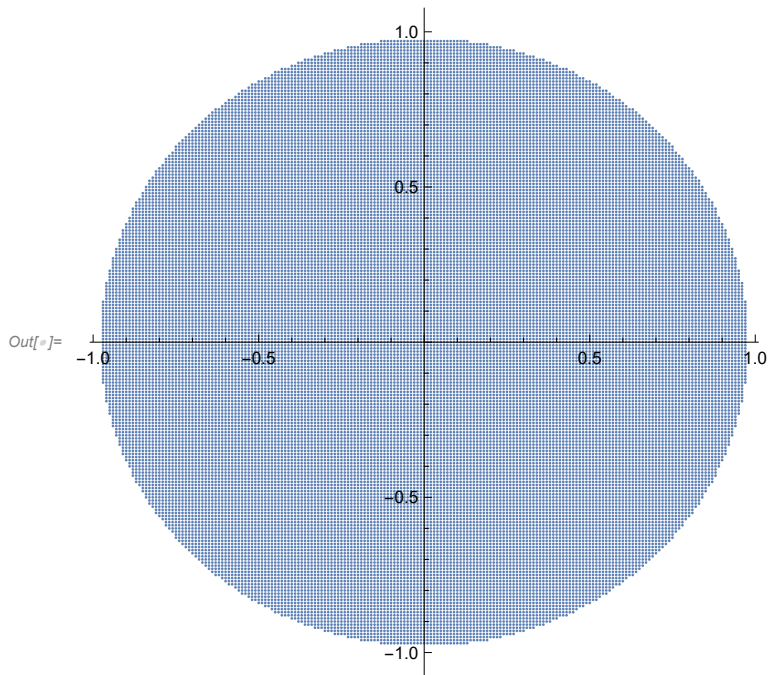
```
Out[ ]//MatrixForm=
```

$$\begin{pmatrix} 0.941077 + 0. i & -0.204803 + 0.0294567 i \\ -0.204803 - 0.0294567 i & 0.0589231 + 0. i \end{pmatrix}$$

```
In[ ]:= step3 = 0.01;
```

```
In[ ]:= coordinates3 = Select[Flatten[Table[{x, y}, {x, -1, 1, step3}, {y, -1, 1, step3}], 1],  
PositiveSemidefiniteMatrixQ[1/2 * (Flatten[{1, #, 0.2}]).SaMPB[2]] &];
```

```
In[ ]:= ListPlot[coordinates3, AspectRatio -> 1]
```



```
In[ ]:= Cost3 = CostfromObservable[
```

```
{RandSelfadjMatrix[2], RandSelfadjMatrix[2], RandSelfadjMatrix[2]}, True]
```

```
Out[ ]:= { {12.9344 + 0. i, 0.207107 + 0.371762 i, 0.207107 - 0.371762 i, -12.9344 + 0. i},  
{0.207107 - 0.371762 i, 57.2756 + 0. i, -12.6113 + 1.07134 i, -0.207107 + 0.371762 i},  
{0.207107 + 0.371762 i, -12.6113 - 1.07134 i, 57.2756 + 0. i, -0.207107 - 0.371762 i},  
{-12.9344 + 0. i, -0.207107 - 0.371762 i, -0.207107 + 0.371762 i, 12.9344 + 0. i} }
```

```
In[ ]:= % // MatrixForm
```

```
Out[ ]//MatrixForm=
```

$$\begin{pmatrix} 12.9344 + 0. i & 0.207107 + 0.371762 i & 0.207107 - 0.371762 i & -12.9344 + 0. i \\ 0.207107 - 0.371762 i & 57.2756 + 0. i & -12.6113 + 1.07134 i & -0.207107 + 0.371762 i \\ 0.207107 + 0.371762 i & -12.6113 - 1.07134 i & 57.2756 + 0. i & -0.207107 - 0.371762 i \\ -12.9344 + 0. i & -0.207107 - 0.371762 i & -0.207107 + 0.371762 i & 12.9344 + 0. i \end{pmatrix}$$

```
In[ ]:=  $\omega_3 = 1/2 * (\text{Flatten}[\{1, \#, 0.2\}]) . \text{SaMPB}[2] \& /@ \text{coordinates3};$ 
```

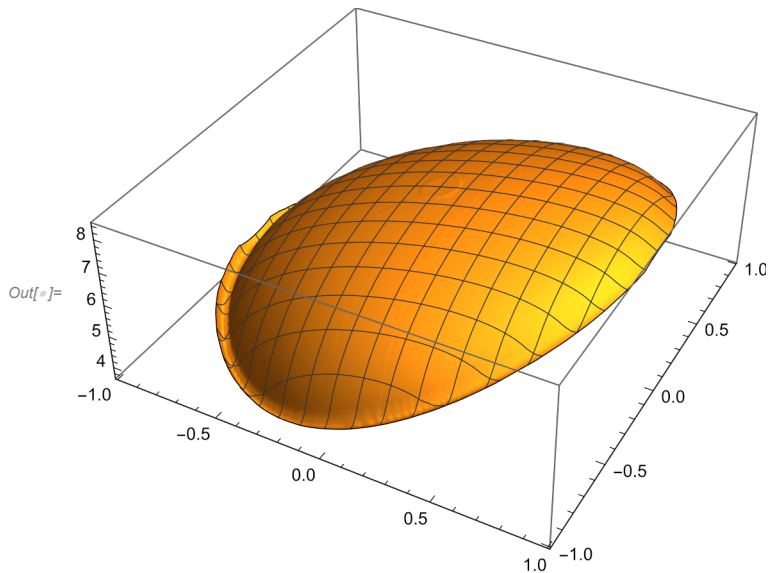
```
In[ ]:= Off[SemidefiniteOptimization::parsuc]
```

```
In[ ]:= {time3, result3} = AbsoluteTiming[TriIneq[ $\rho_3$ , #,  $\tau_3$ , Cost3, False, True] & /@  $\omega_3$ ];
```

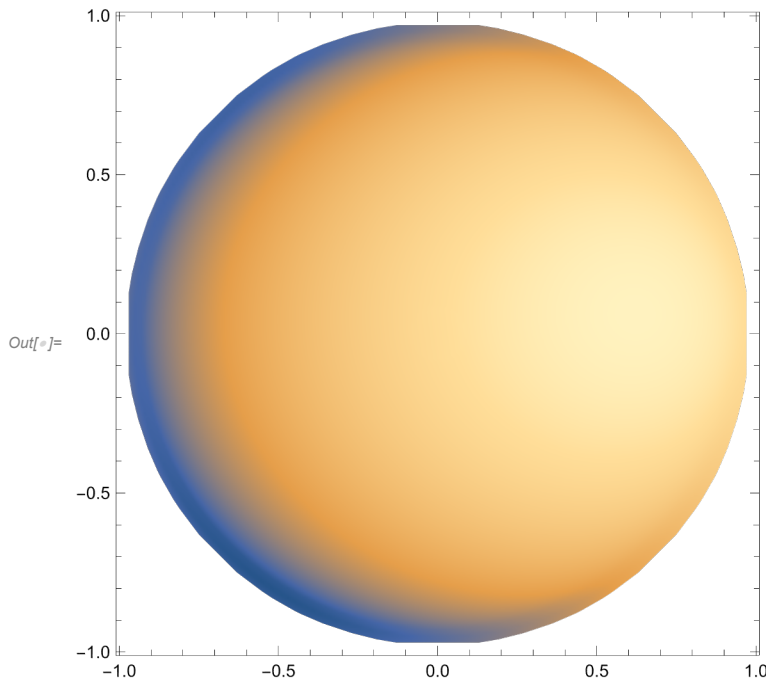
```
In[ ]:= time3 / 3600
```

```
Out[ ]:= 1.42924
```

```
In[5]:= ListPlot3D[Join[coordinates3, Transpose@{result3}, 2]]
```



```
In[ ]:= ListDensityPlot[Join[coordinates3, Transpose@{result3}, 2]]
```



```
In[ ]:= Max[Abs[Im[result3]]]
```

```
Out[ ]:= 0
```

```
In[ ]:= Min[result3]
```

```
Out[ ]:= 3.71871
```

```
In[ ]:= ρ04 = RandState[4, 4]
```

```
Out[ ]:= {{0.0718617 + 0. i, -0.0388539 + 0.112849 i,
           -0.0649472 + 0.0410115 i, -0.0329795 - 0.0212718 i},
          {-0.0388539 - 0.112849 i, 0.432019 + 0. i, 0.141496 - 0.0000971459 i, 0.0452387 + 0.0594228 i},
          {-0.0649472 - 0.0410115 i, 0.141496 + 0.0000971459 i,
           0.303302 + 0. i, 0.0650013 - 0.0223743 i},
          {-0.0329795 + 0.0212718 i, 0.0452387 - 0.0594228 i, 0.0650013 + 0.0223743 i, 0.192817 + 0. i}}
```

```
In[ ]:= % // MatrixForm
```

```
Out[ ]:= MatrixForm=

$$\begin{pmatrix} 0.0718617 + 0. i & -0.0388539 + 0.112849 i & -0.0649472 + 0.0410115 i & -0.0329795 - 0.0212718 i \\ -0.0388539 - 0.112849 i & 0.432019 + 0. i & 0.141496 - 0.0000971459 i & 0.0452387 + 0.0594228 i \\ -0.0649472 - 0.0410115 i & 0.141496 + 0.0000971459 i & 0.303302 + 0. i & 0.0650013 - 0.0223743 i \\ -0.0329795 + 0.0212718 i & 0.0452387 - 0.0594228 i & 0.0650013 + 0.0223743 i & 0.192817 + 0. i \end{pmatrix}$$

```

```
In[ ]:=  $\tau$ 04 = RandState[4, 4]
```

```
Out[ ]:= { {0.187318 + 0. i, 0.0431051 + 0.0604621 i, -0.067781 - 0.0548287 i, 0.0264342 - 0.172235 i},
  {0.0431051 - 0.0604621 i, 0.281131 + 0. i, -0.0906402 + 0.0201966 i, -0.0152662 - 0.0305359 i},
  {-0.067781 + 0.0548287 i, -0.0906402 - 0.0201966 i,
  0.101031 + 0. i, -0.00417941 + 0.0149378 i},
  {0.0264342 + 0.172235 i, -0.0152662 + 0.0305359 i, -0.00417941 - 0.0149378 i, 0.43052 + 0. i} }
```

```
In[ ]:= % // MatrixForm
```

```
Out[ ]//MatrixForm=

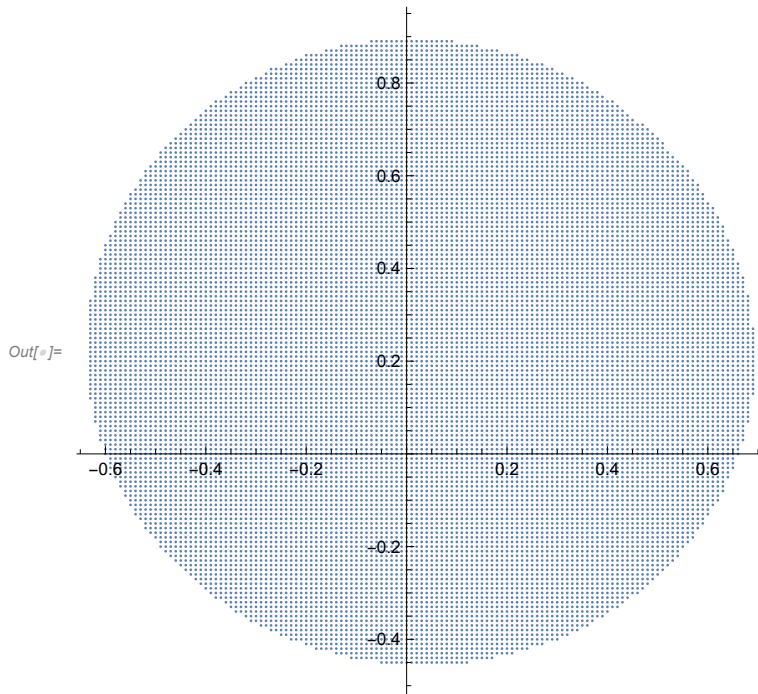
$$\begin{pmatrix} 0.187318 + 0. i & 0.0431051 + 0.0604621 i & -0.067781 - 0.0548287 i & 0.0264342 - 0.172235 i \\ 0.0431051 - 0.0604621 i & 0.281131 + 0. i & -0.0906402 + 0.0201966 i & -0.0152662 - 0.0305359 i \\ -0.067781 + 0.0548287 i & -0.0906402 - 0.0201966 i & 0.101031 + 0. i & -0.00417941 + 0.0149378 i \\ 0.0264342 + 0.172235 i & -0.0152662 + 0.0305359 i & -0.00417941 - 0.0149378 i & 0.43052 + 0. i \end{pmatrix}$$

```

```
In[ ]:= step4 = 0.01;
```

```
In[ ]:= coordinates4 = Select[Flatten[Table[{x, y}, {x, -1, 1, step4}, {y, -1, 1, step4}], 1],
  PositiveSemidefiniteMatrixQ[
    1 / 4 * (Flatten[{1, #, 0, 0.1, 0.1, 0.1, 0, 0.3, 0, 0.2, 0, 0, 0, 0, 0}]) . SaMPB[4]] &];
```

```
In[ ]:= ListPlot[coordinates4, AspectRatio -> 1]
```



```
In[ ]:= Cost4 = CostfromObservable[{RandSelfadjMatrix[4], RandSelfadjMatrix[4],
  RandSelfadjMatrix[4], RandSelfadjMatrix[4], RandSelfadjMatrix[4]}, True];
```

```
In[ ]:= Round[Cost4, 1] // MatrixForm
```

```
Out[ ]//MatrixForm=
```

75	-5 i	10 + 16 i	6 - 6 i	5 i	-22	10 - i	9 - 2 i	10 - 16 i	10
5 i	108	16 + 9 i	2 + 8 i	5 - 2 i	12 + 8 i	-4 + 12 i	3 - 6 i	7 - 12 i	-4
10 - 16 i	16 - 9 i	171	-34 - 18 i	7 - 12 i	6 - 9 i	14 - 15 i	-11 - 6 i	-10 + 15 i	2 +
6 + 6 i	2 - 8 i	-34 + 18 i	113	7 i	-6 + 12 i	-8	2 - 8 i	-11 - 6 i	-4
-5 i	5 + 2 i	7 + 12 i	-7 i	108	12 - 8 i	-4 + 4 i	-4 + 6 i	16 - 9 i	-4 -
-22	12 - 8 i	6 + 9 i	-6 - 12 i	12 + 8 i	92	-5	-7 + 12 i	6 - 9 i	-
10 + i	-4 - 12 i	14 + 15 i	-8	-4 - 4 i	-5	140	-12 - 21 i	2 + 7 i	-1
9 + 2 i	3 + 6 i	-11 + 6 i	2 + 8 i	-4 - 6 i	-7 - 12 i	-12 + 21 i	124	-2 + 11 i	-1!
10 + 16 i	7 + 12 i	-10 - 15 i	-11 + 6 i	16 + 9 i	6 + 9 i	2 - 7 i	-2 - 11 i	171	14 +
10 - i	-4 + 4 i	2 - 7 i	-4 + 6 i	-4 + 12 i	-5	-1 - 8 i	-15 - i	14 - 15 i	1
-25	12 i	-18 - 10 i	-1 + 13 i	-12 i	-46	-1 + 17 i	7 - 15 i	-18 + 10 i	-1 -
2 - 15 i	8 - 11 i	18 + 10 i	-2 + 2 i	1 + 3 i	10 + 18 i	-11 + 22 i	17 + 25 i	-8 - 6 i	-13
6 - 6 i	-7 i	-11 + 6 i	21 + 11 i	2 + 8 i	-6 - 12 i	-4 + 6 i	7 + 12 i	-34 - 18 i	-
9 - 2 i	-4 + 6 i	-2 - 11 i	7 + 12 i	3 - 6 i	-7 + 12 i	-15 - i	8 - 7 i	-11 - 6 i	-12
2 + 15 i	1 - 3 i	-8 + 6 i	15 - 6 i	8 + 11 i	10 - 18 i	-13 + 8 i	15 - 7 i	18 - 10 i	-11
-29	-11 + i	3 - 14 i	1 + 6 i	-11 - i	-25	-4 - 16 i	-9 + 5 i	3 + 14 i	-4 +

```
In[ ]:=  $\omega4 = 1 / 4 * (\text{Flatten}[\{1, \#, 0, 0.1, 0.1, 0.1, 0, 0.3, 0, 0.2, 0, 0, 0, 0\}]) . \text{SaMPB}[4] \& / @$   
coordinates4;
```

```
In[ ]:= Off[SemidefiniteOptimization::parsuc]
```

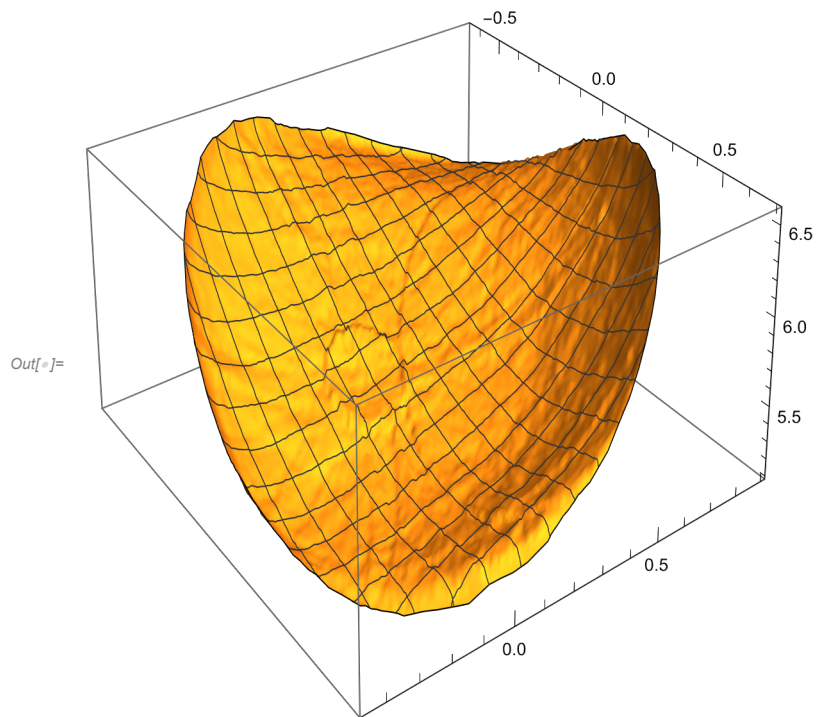
```
In[ ]:= {time4, result4} = AbsoluteTiming[TriIneq[ $\rho04$ , #,  $\tau04$ , Cost4, False, True] & /@  $\omega4$ ];
```

```
In[ ]:= time4 / 3600
```

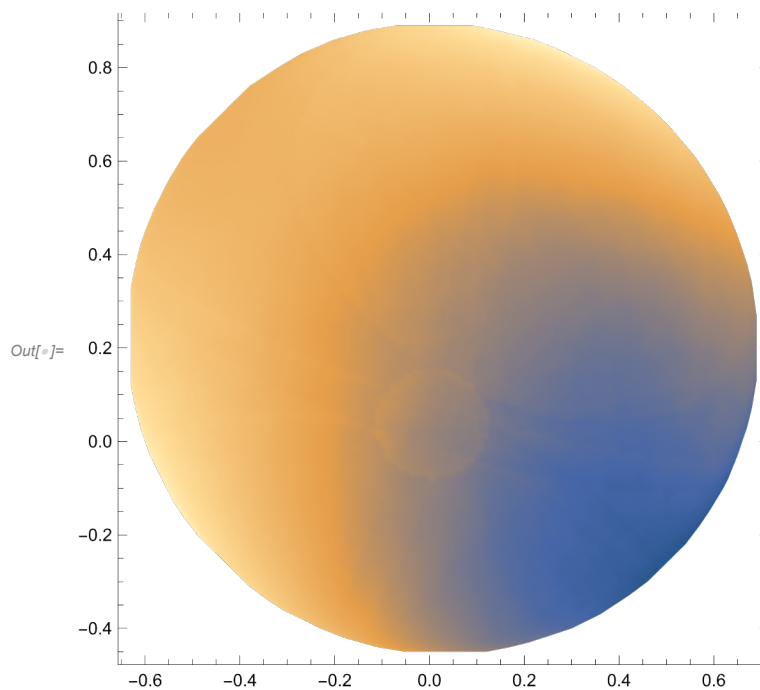
```
Out[ ]:= 12.4241
```



```
In[4]:= ListPlot3D[Join[coordinates4, Transpose@{result4}, 2], AspectRatio -> 1]
```



```
In[5]:= ListDensityPlot[Join[coordinates4, Transpose@{result4}, 2], AspectRatio -> 1]
```



```
In[6]:= Max[Abs[Im[result4]]]
```

Out[6]= 0

```
In[ ]:= Min[result4]
```

```
Out[ ]:= 5.11249
```
