

#### HW4 Due on Oct 8

1\*. Let  $G$  be a triangle-free graph of at most 10 vertices. Show that  $\chi(G) \leq 3$ .

2. Let  $G$  be an arbitrary graph of  $n$  vertices and  $\overline{G}$  be the complement of  $G$ . Show that  $\chi(G)\chi(\overline{G}) \geq n$ .

3\*. Let  $G$  be an arbitrary graph of  $n$  vertices and  $\overline{G}$  be the complement of  $G$ . Show that  $\chi(G) + \chi(\overline{G}) \leq n + 1$ .